

## organic compounds



Acta Crystallographica Section E

## Structure Reports

Online

ISSN 1600-5368

4-(2-Azaniumylethyl)piperazin-1-ium  
bis(perchlorate)Mohammad Reza Reisi,<sup>a</sup> Muhammad Saleh Salga,<sup>b</sup> Hamid  
Khaledi<sup>b\*</sup> and Hapipah Mohd Ali<sup>b</sup><sup>a</sup>Chemistry Department, Isfahan University, 81646-73441 Isfahan, Iran, and<sup>b</sup>Department of Chemistry, University of Malaya, 50603 Kuala Lumpur, MalaysiaCorrespondence e-mail: [khaledi@siswa.um.edu.my](mailto:khaledi@siswa.um.edu.my)

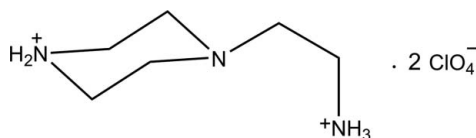
Received 12 August 2011; accepted 19 August 2011

Key indicators: single-crystal X-ray study;  $T = 100$  K; mean  $\sigma(\text{C}-\text{C}) = 0.002$  Å;  
 $R$  factor = 0.030;  $wR$  factor = 0.080; data-to-parameter ratio = 15.9.

In the title compound,  $\text{C}_6\text{H}_{17}\text{N}_3^{2+} \cdot 2\text{ClO}_4^-$ , the piperazine ring adopts a chair conformation with the ethylammonium fragment occupying an equatorial position. In the crystal, the dications and perchlorate anions are linked through  $\text{N}-\text{H} \cdots \text{O}$  hydrogen bonding and weak  $\text{C}-\text{H} \cdots \text{O}$  hydrogen bonding into a three-dimensional supramolecular network.

## Related literature

For the structures of related salts of the 4-(2-ammonioethyl)piperazin-1-ium cation, see: Guerfel *et al.* (1999); Srinivasan *et al.* (2008, 2009).



## Experimental

## Crystal data

 $\text{C}_6\text{H}_{17}\text{N}_3^{2+} \cdot 2\text{ClO}_4^-$  $M_r = 330.13$ Monoclinic,  $P2_1/n$  $a = 7.5218$  (1) Å $b = 11.4371$  (2) Å $c = 15.2239$  (2) Å $\beta = 97.437$  (1)° $V = 1298.66$  (3) Å<sup>3</sup> $Z = 4$ Mo  $K\alpha$  radiation $\mu = 0.54$  mm<sup>-1</sup> $T = 100$  K $0.28 \times 0.17 \times 0.06$  mm

## Data collection

Bruker APEXII CCD

diffractometer

Absorption correction: multi-scan

(SADABS; Sheldrick, 1996)

 $T_{\min} = 0.863$ ,  $T_{\max} = 0.968$ 

8644 measured reflections

2969 independent reflections

2671 reflections with  $I > 2\sigma(I)$  $R_{\text{int}} = 0.023$ 

## Refinement

 $R[F^2 > 2\sigma(F^2)] = 0.030$  $wR(F^2) = 0.080$  $S = 1.05$ 

2969 reflections

187 parameters

5 restraints

H atoms treated by a mixture of independent and constrained refinement

 $\Delta\rho_{\max} = 0.27$  e Å<sup>-3</sup> $\Delta\rho_{\min} = -0.59$  e Å<sup>-3</sup>

Table 1

Hydrogen-bond geometry (Å, °).

$D-H \cdots A$	$D-H$	$H \cdots A$	$D \cdots A$	$D-H \cdots A$
$\text{N1}-\text{H1C} \cdots \text{O4}^{\text{i}}$	0.90 (2)	2.16 (2)	2.9298 (19)	143 (2)
$\text{N1}-\text{H1D} \cdots \text{O3}^{\text{ii}}$	0.88 (2)	2.09 (2)	2.964 (2)	168 (2)
$\text{N3}-\text{H3C} \cdots \text{O6}^{\text{i}}$	0.89 (2)	2.38 (2)	3.0741 (19)	135 (2)
$\text{N3}-\text{H3C} \cdots \text{O4}$	0.89 (2)	2.39 (2)	3.0225 (19)	128 (2)
$\text{N3}-\text{H3D} \cdots \text{O1}^{\text{iii}}$	0.89 (2)	2.12 (2)	2.9875 (18)	163 (2)
$\text{N3}-\text{H3E} \cdots \text{O8}^{\text{iv}}$	0.88 (2)	2.14 (2)	2.9025 (19)	145 (2)
$\text{N3}-\text{H3E} \cdots \text{O3}$	0.88 (2)	2.52 (2)	3.0724 (19)	122 (2)
$\text{C1}-\text{H1B} \cdots \text{O7}^{\text{v}}$	0.99	2.56	3.407 (2)	143
$\text{C3}-\text{H3A} \cdots \text{O8}^{\text{iii}}$	0.99	2.56	3.226 (2)	124
$\text{C5}-\text{H5A} \cdots \text{O5}^{\text{vi}}$	0.99	2.58	3.436 (2)	145
$\text{C5}-\text{H5B} \cdots \text{O2}^{\text{iii}}$	0.99	2.46	3.452 (2)	178

Symmetry codes: (i)  $-x+1, -y+1, -z+1$ ; (ii)  $x-\frac{1}{2}, -y+\frac{1}{2}, z-\frac{1}{2}$ ; (iii)  $x-1, y, z$ ; (iv)  $x-\frac{1}{2}, -y+\frac{1}{2}, z+\frac{1}{2}$ ; (v)  $-x+\frac{1}{2}, y-\frac{1}{2}, -z+\frac{1}{2}$ ; (vi)  $-x+\frac{1}{2}, y-\frac{1}{2}, -z+\frac{1}{2}$ .

Data collection: APEX2 (Bruker, 2007); cell refinement: SAINT (Bruker, 2007); data reduction: SAINT; program(s) used to solve structure: SHELXS97 (Sheldrick, 2008); program(s) used to refine structure: SHELXL97 (Sheldrick, 2008); molecular graphics: X-SEED (Barbour, 2001); software used to prepare material for publication: SHELXL97 and publCIF (Westrip, 2010).

The authors thank the University of Malaya for funding this study (PPP grant No. PS359/2009C).

Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: XU5296).

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**supplementary materials**

*Acta Cryst.* (2011). E67, o2400 [ doi:10.1107/S1600536811033976 ]

## 4-(2-Azaniumylethyl)piperazin-1-ium bis(perchlorate)

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### Comment

The crystals of the title compound were obtained unexpectedly during an attempt to prepare a tin(IV) complex of 1-(2-aminoethyl)piperazine in the presence of sodium perchlorate. The organic molecule is doubly protonated at its primary and secondary N atoms, while the tertiary N atom, N2, remains unprotonated. Similar to the structures of some other 1-(2-ammoniummethyl)piperazinium salts (Guerfel *et al.*, 1999; Srinivasan *et al.*, 2008, 2009), the piperazine ring adopts a chair conformation with the ethylammonium group occupying an equatorial position. In the crystal, the dicationic organic moieties and perchlorate anions are linked through N—H $\cdots$ O and C—H $\cdots$ O interactions (Table 1) into a three-dimensional supra-molecular network.

### Experimental

A mixture of 4-(2-aminoethyl)piperazine (0.26 g, 2 mmol) and Bu<sub>2</sub>SnCl<sub>2</sub> (0.6 g, 2 mmol) in methanol (50 ml) was refluxed for 2 h. NaClO<sub>4</sub> (0.56 g, 4 mmol) was then added and the precipitated sodium chloride was filtered off. The filtrate was evaporated and the obtained solid was recrystallized from ethanol at room temperature to give the colorless crystals of the title compound.

### Refinement

The C-bound H atoms were placed at calculated positions and were treated as riding on their parent C atoms with C—H = 0.99 Å. The N-bound H atoms were located in a difference Fourier map, and refined with distance restraints of N—H = 0.91 (2) Å. For all H atoms,  $U_{\text{iso}}(\text{H})$  was set to  $1.2U_{\text{eq}}(\text{carrier atom})$ .

### Figures

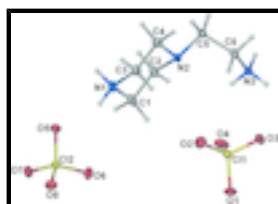
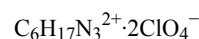


Fig. 1. Molecular structure of the title compound with thermal ellipsoids at the 50% probability level. H atoms are drawn as spheres of arbitrary radius.

## 4-(2-Azaniumylethyl)piperazin-1-ium bis(perchlorate)

### Crystal data



$$M_r = 330.13$$

$$F(000) = 688$$

$$D_x = 1.688 \text{ Mg m}^{-3}$$

# supplementary materials

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Monoclinic,  $P2_1/n$   
Hall symbol: -P 2yn  
 $a = 7.5218$  (1) Å  
 $b = 11.4371$  (2) Å  
 $c = 15.2239$  (2) Å  
 $\beta = 97.437$  (1)°  
 $V = 1298.66$  (3) Å<sup>3</sup>  
 $Z = 4$

Mo  $K\alpha$  radiation,  $\lambda = 0.71073$  Å  
Cell parameters from 4052 reflections  
 $\theta = 2.2$ – $30.5^\circ$   
 $\mu = 0.54$  mm<sup>-1</sup>  
 $T = 100$  K  
Blade, colourless  
 $0.28 \times 0.17 \times 0.06$  mm

## Data collection

Bruker APEXII CCD  
diffractometer  
Radiation source: fine-focus sealed tube  
graphite  
 $\varphi$  and  $\omega$  scans  
Absorption correction: multi-scan  
(*SADABS*; Sheldrick, 1996)  
 $T_{\min} = 0.863$ ,  $T_{\max} = 0.968$   
8644 measured reflections

2969 independent reflections  
2671 reflections with  $I > 2\sigma(I)$   
 $R_{\text{int}} = 0.023$   
 $\theta_{\max} = 27.5^\circ$ ,  $\theta_{\min} = 2.2^\circ$   
 $h = -9 \rightarrow 9$   
 $k = -14 \rightarrow 12$   
 $l = -19 \rightarrow 18$

## Refinement

Refinement on  $F^2$   
Least-squares matrix: full  
 $R[F^2 > 2\sigma(F^2)] = 0.030$   
 $wR(F^2) = 0.080$   
 $S = 1.05$   
2969 reflections  
187 parameters  
5 restraints

Primary atom site location: structure-invariant direct methods  
Secondary atom site location: difference Fourier map  
Hydrogen site location: inferred from neighbouring sites  
H atoms treated by a mixture of independent and constrained refinement  
 $w = 1/[\sigma^2(F_o^2) + (0.0388P)^2 + 0.8608P]$   
where  $P = (F_o^2 + 2F_c^2)/3$   
 $(\Delta/\sigma)_{\max} = 0.001$   
 $\Delta\rho_{\max} = 0.27$  e Å<sup>-3</sup>  
 $\Delta\rho_{\min} = -0.59$  e Å<sup>-3</sup>

## Special details

**Geometry.** All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

**Refinement.** Refinement of  $F^2$  against ALL reflections. The weighted  $R$ -factor  $wR$  and goodness of fit  $S$  are based on  $F^2$ , conventional  $R$ -factors  $R$  are based on  $F$ , with  $F$  set to zero for negative  $F^2$ . The threshold expression of  $F^2 > \sigma(F^2)$  is used only for calculating  $R$ -factors(gt) *etc.* and is not relevant to the choice of reflections for refinement.  $R$ -factors based on  $F^2$  are statistically about twice as large as those based on  $F$ , and  $R$ -factors based on ALL data will be even larger.

*Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\text{\AA}^2$ )*

	<i>x</i>	<i>y</i>	<i>z</i>	<i>U</i> <sub>iso</sub> <sup>*</sup> / <i>U</i> <sub>eq</sub>
N1	0.3280 (2)	0.44351 (13)	0.34193 (10)	0.0188 (3)
H1C	0.390 (3)	0.5105 (15)	0.3389 (14)	0.023 <sup>*</sup>
H1D	0.268 (3)	0.4345 (19)	0.2884 (11)	0.023 <sup>*</sup>
N2	0.22434 (17)	0.25008 (12)	0.44167 (9)	0.0137 (3)
N3	0.26916 (19)	0.16033 (12)	0.61553 (9)	0.0138 (3)
H3C	0.308 (3)	0.2308 (14)	0.6010 (13)	0.017 <sup>*</sup>
H3D	0.161 (2)	0.1729 (17)	0.6323 (13)	0.017 <sup>*</sup>
H3E	0.340 (2)	0.1314 (17)	0.6606 (11)	0.017 <sup>*</sup>
C1	0.4538 (2)	0.34346 (15)	0.36621 (12)	0.0212 (4)
H1A	0.5295	0.3604	0.4229	0.025 <sup>*</sup>
H1B	0.5334	0.3327	0.3199	0.025 <sup>*</sup>
C2	0.3466 (2)	0.23325 (15)	0.37506 (11)	0.0182 (3)
H2A	0.2769	0.2137	0.3173	0.022 <sup>*</sup>
H2B	0.4289	0.1674	0.3928	0.022 <sup>*</sup>
C3	0.1959 (2)	0.45727 (15)	0.40696 (12)	0.0186 (3)
H3A	0.1099	0.5205	0.3873	0.022 <sup>*</sup>
H3B	0.2595	0.4787	0.4658	0.022 <sup>*</sup>
C4	0.0963 (2)	0.34326 (15)	0.41350 (12)	0.0190 (3)
H4A	0.0095	0.3513	0.4568	0.023 <sup>*</sup>
H4B	0.0289	0.3235	0.3552	0.023 <sup>*</sup>
C5	0.1375 (2)	0.13996 (15)	0.46127 (11)	0.0165 (3)
H5A	0.1257	0.0886	0.4085	0.020 <sup>*</sup>
H5B	0.0160	0.1559	0.4768	0.020 <sup>*</sup>
C6	0.2498 (2)	0.08004 (14)	0.53790 (11)	0.0158 (3)
H6A	0.1911	0.0065	0.5529	0.019 <sup>*</sup>
H6B	0.3694	0.0606	0.5214	0.019 <sup>*</sup>
Cl1	0.72577 (5)	0.21252 (3)	0.61138 (3)	0.01391 (10)
O1	0.90644 (15)	0.24485 (11)	0.64617 (9)	0.0220 (3)
O2	0.71413 (18)	0.18723 (12)	0.51861 (8)	0.0263 (3)
O3	0.67246 (17)	0.10996 (11)	0.65736 (9)	0.0241 (3)
O4	0.60538 (16)	0.30697 (11)	0.62494 (10)	0.0246 (3)
Cl2	0.74537 (5)	0.57603 (3)	0.26377 (2)	0.01355 (10)
O5	0.59033 (15)	0.51100 (11)	0.22387 (8)	0.0188 (3)
O6	0.75093 (17)	0.57359 (11)	0.35894 (8)	0.0200 (3)
O7	0.73342 (17)	0.69479 (10)	0.23263 (8)	0.0204 (3)
O8	0.90557 (15)	0.52178 (11)	0.23899 (8)	0.0202 (3)

*Atomic displacement parameters ( $\text{\AA}^2$ )*

	<i>U</i> <sup>11</sup>	<i>U</i> <sup>22</sup>	<i>U</i> <sup>33</sup>	<i>U</i> <sup>12</sup>	<i>U</i> <sup>13</sup>	<i>U</i> <sup>23</sup>
N1	0.0269 (8)	0.0140 (7)	0.0159 (7)	−0.0024 (6)	0.0044 (6)	0.0008 (6)
N2	0.0141 (6)	0.0131 (7)	0.0144 (7)	−0.0002 (5)	0.0034 (5)	0.0015 (5)
N3	0.0150 (6)	0.0119 (7)	0.0147 (7)	−0.0003 (5)	0.0026 (5)	0.0003 (5)
C1	0.0235 (9)	0.0174 (9)	0.0246 (9)	0.0005 (7)	0.0107 (7)	0.0029 (7)

## supplementary materials

C2	0.0227 (8)	0.0158 (8)	0.0178 (8)	−0.0002 (6)	0.0090 (6)	0.0002 (6)
C3	0.0193 (8)	0.0171 (8)	0.0195 (8)	0.0022 (6)	0.0030 (6)	0.0004 (7)
C4	0.0151 (8)	0.0187 (9)	0.0227 (9)	0.0016 (6)	0.0009 (6)	0.0016 (7)
C5	0.0175 (8)	0.0162 (8)	0.0158 (8)	−0.0044 (6)	0.0027 (6)	−0.0009 (6)
C6	0.0190 (8)	0.0125 (8)	0.0164 (8)	−0.0014 (6)	0.0046 (6)	−0.0026 (6)
Cl1	0.01169 (18)	0.01297 (19)	0.0174 (2)	−0.00018 (13)	0.00309 (13)	−0.00125 (14)
O1	0.0125 (6)	0.0229 (7)	0.0300 (7)	−0.0028 (5)	0.0010 (5)	−0.0039 (5)
O2	0.0263 (7)	0.0354 (8)	0.0176 (7)	−0.0007 (6)	0.0045 (5)	−0.0055 (6)
O3	0.0219 (6)	0.0207 (7)	0.0290 (7)	−0.0045 (5)	0.0012 (5)	0.0090 (5)
O4	0.0155 (6)	0.0157 (6)	0.0437 (8)	0.0021 (5)	0.0076 (5)	−0.0067 (6)
Cl2	0.01502 (19)	0.01298 (19)	0.01291 (19)	0.00041 (13)	0.00284 (13)	−0.00077 (13)
O5	0.0160 (6)	0.0196 (6)	0.0206 (6)	−0.0037 (5)	0.0016 (5)	−0.0013 (5)
O6	0.0283 (7)	0.0194 (6)	0.0128 (6)	0.0033 (5)	0.0045 (5)	−0.0001 (5)
O7	0.0274 (7)	0.0134 (6)	0.0207 (6)	−0.0012 (5)	0.0038 (5)	0.0031 (5)
O8	0.0164 (6)	0.0227 (7)	0.0223 (7)	0.0022 (5)	0.0056 (5)	−0.0069 (5)

### *Geometric parameters (Å, °)*

N1—C3	1.499 (2)	C3—H3A	0.9900
N1—C1	1.500 (2)	C3—H3B	0.9900
N1—H1C	0.902 (15)	C4—H4A	0.9900
N1—H1D	0.884 (15)	C4—H4B	0.9900
N2—C4	1.463 (2)	C5—C6	1.513 (2)
N2—C5	1.467 (2)	C5—H5A	0.9900
N2—C2	1.467 (2)	C5—H5B	0.9900
N3—C6	1.489 (2)	C6—H6A	0.9900
N3—H3C	0.894 (15)	C6—H6B	0.9900
N3—H3D	0.894 (15)	Cl1—O2	1.4331 (13)
N3—H3E	0.878 (15)	Cl1—O1	1.4414 (12)
C1—C2	1.512 (2)	Cl1—O4	1.4416 (12)
C1—H1A	0.9900	Cl1—O3	1.4489 (13)
C1—H1B	0.9900	Cl2—O7	1.4376 (12)
C2—H2A	0.9900	Cl2—O6	1.4444 (12)
C2—H2B	0.9900	Cl2—O8	1.4481 (12)
C3—C4	1.513 (2)	Cl2—O5	1.4487 (12)
C3—N1—C1	111.60 (13)	H3A—C3—H3B	108.3
C3—N1—H1C	109.7 (13)	N2—C4—C3	109.53 (13)
C1—N1—H1C	110.3 (13)	N2—C4—H4A	109.8
C3—N1—H1D	108.6 (14)	C3—C4—H4A	109.8
C1—N1—H1D	111.6 (14)	N2—C4—H4B	109.8
H1C—N1—H1D	104.8 (19)	C3—C4—H4B	109.8
C4—N2—C5	113.04 (13)	H4A—C4—H4B	108.2
C4—N2—C2	109.92 (13)	N2—C5—C6	109.07 (13)
C5—N2—C2	111.30 (13)	N2—C5—H5A	109.9
C6—N3—H3C	111.2 (13)	C6—C5—H5A	109.9
C6—N3—H3D	109.1 (13)	N2—C5—H5B	109.9
H3C—N3—H3D	105.1 (18)	C6—C5—H5B	109.9
C6—N3—H3E	112.0 (13)	H5A—C5—H5B	108.3
H3C—N3—H3E	110.4 (18)	N3—C6—C5	108.67 (13)

H3D—N3—H3E	108.8 (18)	N3—C6—H6A	110.0
N1—C1—C2	109.35 (14)	C5—C6—H6A	110.0
N1—C1—H1A	109.8	N3—C6—H6B	110.0
C2—C1—H1A	109.8	C5—C6—H6B	110.0
N1—C1—H1B	109.8	H6A—C6—H6B	108.3
C2—C1—H1B	109.8	O2—C11—O1	110.39 (8)
H1A—C1—H1B	108.3	O2—C11—O4	109.44 (8)
N2—C2—C1	109.97 (14)	O1—C11—O4	109.57 (8)
N2—C2—H2A	109.7	O2—C11—O3	109.10 (8)
C1—C2—H2A	109.7	O1—C11—O3	109.69 (8)
N2—C2—H2B	109.7	O4—C11—O3	108.62 (8)
C1—C2—H2B	109.7	O7—C12—O6	109.97 (7)
H2A—C2—H2B	108.2	O7—C12—O8	109.73 (8)
N1—C3—C4	109.21 (14)	O6—C12—O8	109.63 (7)
N1—C3—H3A	109.8	O7—C12—O5	109.52 (7)
C4—C3—H3A	109.8	O6—C12—O5	109.14 (7)
N1—C3—H3B	109.8	O8—C12—O5	108.82 (7)
C4—C3—H3B	109.8		

*Hydrogen-bond geometry (Å, °)*

<i>D</i> —H $\cdots$ <i>A</i>	<i>D</i> —H	H $\cdots$ <i>A</i>	<i>D</i> $\cdots$ <i>A</i>	<i>D</i> —H $\cdots$ <i>A</i>
N1—H1C $\cdots$ O4 <sup>i</sup>	0.90 (2)	2.16 (2)	2.9298 (19)	143.(2)
N1—H1D $\cdots$ O3 <sup>ii</sup>	0.88 (2)	2.09 (2)	2.964 (2)	168.(2)
N3—H3C $\cdots$ O6 <sup>i</sup>	0.89 (2)	2.38 (2)	3.0741 (19)	135.(2)
N3—H3C $\cdots$ O4	0.89 (2)	2.39 (2)	3.0225 (19)	128.(2)
N3—H3D $\cdots$ O1 <sup>iii</sup>	0.89 (2)	2.12 (2)	2.9875 (18)	163.(2)
N3—H3E $\cdots$ O8 <sup>iv</sup>	0.88 (2)	2.14 (2)	2.9025 (19)	145.(2)
N3—H3E $\cdots$ O3	0.88 (2)	2.52 (2)	3.0724 (19)	122.(2)
C1—H1B $\cdots$ O7 <sup>v</sup>	0.99	2.56	3.407 (2)	143.
C3—H3A $\cdots$ O8 <sup>iii</sup>	0.99	2.56	3.226 (2)	124.
C5—H5A $\cdots$ O5 <sup>vi</sup>	0.99	2.58	3.436 (2)	145.
C5—H5B $\cdots$ O2 <sup>iii</sup>	0.99	2.46	3.452 (2)	178.

Symmetry codes: (i)  $-x+1, -y+1, -z+1$ ; (ii)  $x-1/2, -y+1/2, z-1/2$ ; (iii)  $x-1, y, z$ ; (iv)  $x-1/2, -y+1/2, z+1/2$ ; (v)  $-x+3/2, y-1/2, -z+1/2$ ; (vi)  $-x+1/2, y-1/2, -z+1/2$ .

Fig. 1

